> Jeopardy Game


Solution

|  |  |
| :---: | :---: |
| a | $\ln x+\ln y$ |
| b | $\ln x-\ln y$ |
| c | $x \ln y$ |
| d | $y \ln x$ |
| e | none of them |

The function $y=x^{2} \cdot \sin x$ is

| a |
| :---: |
| b |
| c |

$\arctan 1=$

| a | $\infty$ |
| :---: | :---: |
| b | $\pi$ |
| b | $\overline{3}$ |
| c |  |
|  | $\frac{4}{\pi}$ |
| d | 6 |
| e | none of them |

The equivalence " $a<b$ if and only if $f(a)<f(b)$ " is the property of a even functions
b one-to-one functions
c continuous functions
d increasing functions
e none of them

How many points of inflection is on the graph of the function $y=\sin x$ in the open interval $(0,2 \pi)$

| a | none |
| :--- | :--- |
| b | one |
| c | two |
| d | three |
|  | none of them |

Find points of discontinuity of the function $y=\frac{x-4}{(x-2) \ln x}$

| a | none |
| :---: | :---: |
| b | 0 |
| c | 0, 1 |
| d | 0, 1, 2 |
| e | 0, 2 |
| f | 0, 1, 4 |
| g | 0, 4 |
| h | none of them |

Let $f$ be a function and $f^{-1}$ be its inverse. Then $f^{-1}(f(x))=$

| a | 0 |
| :--- | :--- |
| b | 1 |
|  | $x$ |
| d | $f(x)$ |
| e | $f^{-1}(x)$ |
|  | none of them |

$\arcsin (\sin x)=x$ for every $x \in \mathbf{R}$

| $\sqrt{\mathrm{a}}$ | Yes |
| :--- | :--- |
| b | No |

$\lim _{x \rightarrow-\infty} \operatorname{arctg} x=$

| a | 0 |
| :---: | :---: |
| b | $\underline{\pi}$ |
|  | ${ }^{2} \pi$ |
| c | $\overline{2}$ |
| d | $\infty$ |
| e | $-\infty$ |
| f | none of them |

$\lim \sin x=$ $x \rightarrow \infty$

| a | 1 |
| :--- | :--- |
| b | -1 |
| c | does not exist <br> y |
|  | none of them |

$$
\lim _{x \rightarrow \infty} \frac{2 x^{3}+x^{2}+4}{x^{2}-x+2}=
$$

| y | $\infty$ |
| :--- | :--- |
| b | 2 |
| c | 0 |
| d | none of them |

$$
\begin{aligned}
& \lim _{x \rightarrow 0^{+}} \frac{e^{1 / x}(x-1)}{x} \\
& \hline \mathrm{a} \\
& \hline \mathrm{~b} \\
& \hline \mathrm{c} \\
& \hline \mathrm{~d} \\
& \hline \mathrm{~d} \\
& \hline \mathrm{e} \\
& \hline \mathrm{f} \\
& \hline \mathrm{~g} \\
& \hline \mathrm{~h} \\
& \hline
\end{aligned}
$$

D

$$
\begin{aligned}
& \left(\frac{1}{\sqrt[3]{x}}\right)^{\prime}= \\
& \begin{array}{ll}
\mathrm{a} & \frac{1}{3} x^{-2 / 3} \\
\text { (b } & -\frac{1}{3} x^{-2 / 3} \\
\text { (c } & -\frac{1}{3} x^{1 / 3} \\
\hline \mathrm{~d} & \frac{1}{3} x^{-4 / 3} \\
\hline \mathrm{e} & -\frac{1}{3} x^{-4 / 3}
\end{array}
\end{aligned}
$$

$f$ none of them

$$
(x-x \ln x)^{\prime}=
$$

| a | $\ln x$ |
| :--- | :--- |
| b | $-\ln x$ |
| c | $1+\ln x$ |
| d | $1-\ln x$ |
| e | 0 |
| f | $1-\frac{1}{x}$ |
|  |  |

g none of them

$$
\begin{aligned}
& \left(x^{2} e^{x^{2}}\right)^{\prime} \\
& \begin{array}{|ll}
\hline \mathrm{a} & 2 x e^{2 x} \\
\hline \mathrm{~b} & 2 x e^{x^{2}} 2 x \\
\hline \frac{\mathrm{c}}{\mathrm{~d}} & 2 x e^{x^{2}}+x^{2} e^{x^{2}} \\
\hline \mathrm{~d} & 2 x e^{x^{2}}+x^{2} e^{x^{2}} 2 x \\
\hline \mathrm{e} & 2 x e^{x^{2}} 2 x+x^{2} e^{x^{2}} 2 x \\
\hline \mathrm{f} & \begin{array}{l}
\text { none of them }
\end{array}
\end{array}
\end{aligned}
$$

## D

The definition of the derivative of the function $f$ at the point $a$ is
$\sqrt{\mathrm{a}} \lim _{h \rightarrow 0} \frac{f(x+h)+f(x)}{h}$
(b) $\lim _{h \rightarrow 0} \frac{f(x+h)}{h}$
c $\lim _{h \rightarrow 0} \frac{f(x+h)-f(x)}{h}$
d $\lim _{h \rightarrow 0} \frac{f(x)-f(x+h)}{h}$
$\sqrt{\mathrm{e}} \lim _{h \rightarrow 0} \frac{f(x-h)-f(x)}{h}$
$f$ none of them



## E




By theorem of Bolzano, the polynomial $y=x^{3}+2 x+4$ has zero on

| a | $(0,1)$ |
| :--- | :--- | :--- |
| b | $(1,2)$ |
| c | $(2,3)$ |
|  | $(-1,0)$ |
| e | $(-2,-1)$ |
|  | $(-3,-2)$ |
|  | g <br> none of them |

Let $a \in \operatorname{Im}(f)$. Then the solution of the equation $f(x)=a$ exists. This solution is unique if and only if

a $f$ is one-to-one<br>b $\quad f$ is increasing<br>$f$ continuous<br>$f$ differentiable<br>none of them

If the function has a derivative at the point $x=a$, then it is
a increasing at $a$.
decreasing at $a$. one-to-one at $a$. continuous at $a$. undefined at $a$.

## F

If both $y(a)=y^{\prime}(a)=y^{\prime \prime}(a)=0$, then the function
a has local maximum at $a$.
b has local minimum at $a$.
c has point of inflection at $a$.
d any of these possibilites may be true, we need more informations.

